

Name _____

By writing or printing my name in the space above, I hereby affirm that I have neither given nor received assistance in preparing solutions for this exam.

EE 2240

Exam #1

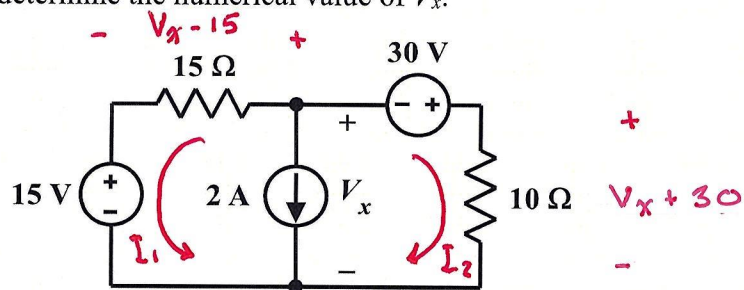
Due by 9:15AM, Tuesday, September 28, 2021

[open book, open notes, calculator and computer allowed – no internet access]

Work must be neat, orderly, and complete in order to receive partial credit.

PLEASE submit your solutions as a single PDF file.

1. Use any method to determine the numerical value of V_x .



$$I_1 = \frac{V_x - 15}{15}$$

$$I_2 = \frac{V_x + 30}{10}$$

$$I_1 + 2 + I_2 = 0$$

$$\Rightarrow \frac{V_x - 15}{15} + 2 + \frac{V_x + 30}{10} = 0$$

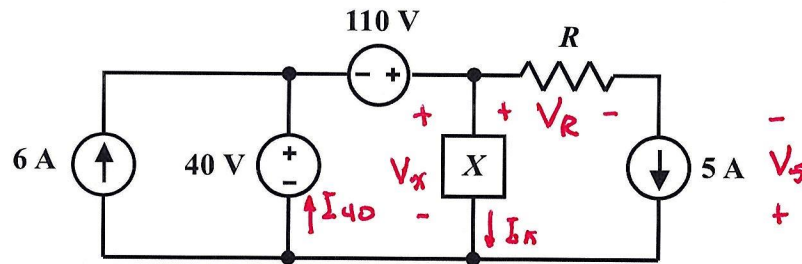
multiply through by 30:

$$2(V_x - 15) + 30(2) + 3(V_x + 30) = 0$$

$$5V_x = -120$$

$$V_x = -\frac{120}{5} = -24 \text{ V}$$

2. The 5A independent current source is delivering 100W, and the 40V independent voltage source is delivering 500W.



- a. Determine the value of resistor R .

$$V_5 (5A) = 100 \text{ W} \Rightarrow V_5 = 20 \text{ V}$$

$$V_R = 110 \text{ V} + 40 \text{ V} + V_5 = 170 \text{ V}$$

$$R = \frac{V_R}{5A} = \frac{170 \text{ V}}{5A} = 34 \Omega$$

- b. Is component X absorbing power or delivering power? How much?

$$(40\text{V}) I_{40} = 500 \text{ W} \Rightarrow I_{40} = 12.5 \text{ A}$$

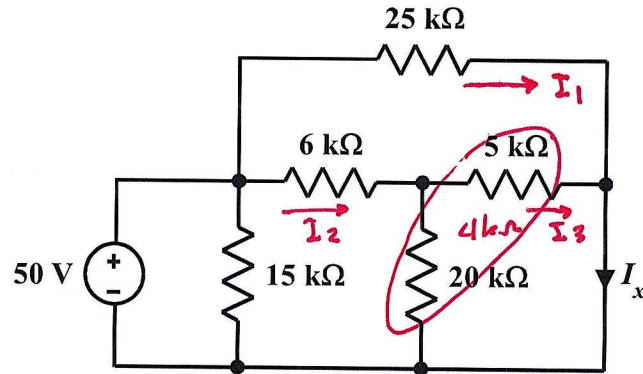
$$I_X = 6 \text{ A} + I_{40} - 5 \text{ A} = 13.5 \text{ A}$$

$$V_X = V_R - V_5 = 150 \text{ V}$$

V_X and I_X satisfy the Passive Sign Convention

$$\Rightarrow X \text{ absorbs } (150\text{V})(13.5\text{A}) = 2025 \text{ W}$$

3. Determine the numerical value of the current I_x .



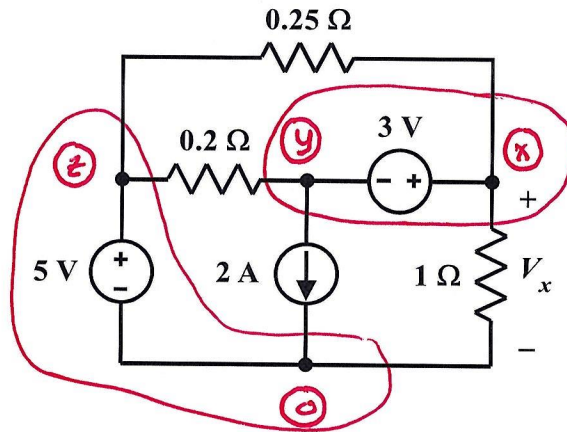
$$I_1 = \frac{50V}{25k\Omega} = 2\text{ mA}$$

$$I_2 = \frac{50V}{6k\Omega + 4k\Omega} = 5\text{ mA}$$

$$I_3 = \frac{20k\Omega}{20k\Omega + 5k\Omega} \cdot I_2 = 4\text{ mA}$$

$$I_x = I_1 + I_3 = 6\text{ mA}$$

4. Use the nodal analysis method to formulate a system of simultaneous linear equations representing the circuit shown, that can be solved to determine the numerical value of V_x directly.



$$V_x - V_y = 3V$$

$$V_z = 5V$$

$$\frac{V_x - V_z}{0.25\Omega} + \frac{V_y - V_z}{0.2\Omega} + 2A + \frac{V_x}{1\Omega} = 0$$

- a. Express the equations in the matrix form discussed in class.

$$\begin{bmatrix} 1 & -1 & 0 \\ 0 & 0 & 1 \\ 5 & 5 & -9 \end{bmatrix} \begin{bmatrix} V_x \\ V_y \\ V_z \end{bmatrix} = \begin{bmatrix} 3 \\ 5 \\ -2 \end{bmatrix}$$

- b. Solve the equations to determine the numerical value of V_x .

$$V_x = \frac{\begin{vmatrix} 3 & -1 & 0 \\ 5 & 0 & 1 \\ -2 & 5 & -9 \end{vmatrix}}{\begin{vmatrix} 1 & -1 & 0 \\ 0 & 0 & 1 \\ 5 & 5 & -9 \end{vmatrix}} = \frac{2 - 45 - 15}{-5 - 5} = 5.8 V$$